

# Tennessee's State Mathematics Standards | Advanced Algebra and Trigonometry

Number and Quantity	Domain	Cluster	Standard
	Number Expressions (N-NE)	Represent, interpret, compare, and simplify number expressions.	<ol style="list-style-type: none"> <li>1. Use the laws of exponents and logarithms to expand or collect terms in expressions; simplify expressions or modify them in order to analyze them or compare them.</li> <li>2. Understand the inverse relationship between exponents and logarithms and use this relationship to solve problems involving logarithms and exponents.*</li> <li>3. Classify real numbers and order real numbers that include transcendental expressions, including roots and fractions of pi and e.</li> <li>4. Simplify complex radical and rational expressions; discuss and display understanding that rational numbers are dense in the real numbers and the integers are not.</li> <li>5. Understand that rational expressions form a system analogous to the rational numbers, closed under addition, subtraction, multiplication, and division by a nonzero rational expression; add, subtract, multiply, and divide rational expressions.</li> </ol>
	Complex numbers (N-CN)	Perform complex number arithmetic and understand the representation on the complex plane.	<ol style="list-style-type: none"> <li>1. Perform arithmetic operations with complex numbers expressing answers in the form <math>a+bi</math>.</li> <li>2. Find the conjugate of a complex number; use conjugates to find moduli and quotients of complex numbers.</li> <li>3. Represent complex numbers on the complex plane in rectangular and polar form (including real and imaginary numbers), and explain why the rectangular and polar forms of a given complex number represent the same number.</li> <li>4. Represent addition, subtraction, multiplication, and conjugation of complex numbers geometrically on the complex plane; use properties of this representation for computation. <i>For example, <math>(-1 + \sqrt{3}i)^3 = 8</math> because <math>(-1 + \sqrt{3}i)</math> has modulus 2 and argument <math>120^\circ</math>.</i></li> <li>5. Calculate the distance between numbers in the complex plane as the modulus of the difference, and the midpoint of a segment as the average of the numbers at its endpoints.</li> </ol>
	Use complex numbers in polynomial identities and equations.	<ol style="list-style-type: none"> <li>6. Extend polynomial identities to the complex numbers. <i>For example, rewrite <math>x^2 + 4</math> as <math>(x + 2i)(x - 2i)</math>.</i></li> <li>7. Know the Fundamental Theorem of Algebra; show that it is true for quadratic polynomials.</li> </ol>	

# Number and Quantity

Domain	Cluster	Standard
<b>Vector and Matrix Quantities (N-VM)</b>	<b>Represent and model with vector quantities.</b>	<ol style="list-style-type: none"> <li>1. Recognize vector quantities as having both magnitude and direction. Represent vector quantities by directed line segments, and use appropriate symbols for vectors and their magnitudes (e.g., <math>\mathbf{v}</math>, <math> \mathbf{v} </math>, <math>\ \mathbf{v}\ </math>, <math>v</math>).</li> <li>2. Find the components of a vector by subtracting the coordinates of an initial point from the coordinates of a terminal point.</li> <li>3. Solve problems involving velocity and other quantities that can be represented by vectors.</li> </ol>
	<b>Understand the graphic representation of vectors and vector arithmetic.</b>	<ol style="list-style-type: none"> <li>4. Add and subtract vectors.               <ol style="list-style-type: none"> <li>a. Add vectors end-to-end, component-wise, and by the parallelogram rule. Understand that the magnitude of a sum of two vectors is typically not the sum of the magnitudes.</li> <li>b. Given two vectors in magnitude and direction form, determine the magnitude and direction of their sum.</li> <li>c. Understand vector subtraction <math>\mathbf{v} - \mathbf{w}</math> as <math>\mathbf{v} + (-\mathbf{w})</math>, where <math>-\mathbf{w}</math> is the additive inverse of <math>\mathbf{w}</math>, with the same magnitude as <math>\mathbf{w}</math> and pointing in the opposite direction. Represent vector subtraction graphically by connecting the tips in the appropriate order, and perform vector subtraction component-wise.</li> </ol> </li> <li>5. Multiply a vector by a scalar.               <ol style="list-style-type: none"> <li>a. Represent scalar multiplication graphically by scaling vectors and possibly reversing their direction; perform scalar multiplication component-wise, e.g., as <math>c(v_x, v_y) = (cv_x, cv_y)</math>.</li> <li>b. Compute the magnitude of a scalar multiple <math>c\mathbf{v}</math> using <math>\ c\mathbf{v}\  =  c v</math>. Compute the direction of <math>c\mathbf{v}</math> knowing that when <math> c v \neq 0</math>, the direction of <math>c\mathbf{v}</math> is either along <math>\mathbf{v}</math> (for <math>c &gt; 0</math>) or against <math>\mathbf{v}</math> (for <math>c &lt; 0</math>).</li> </ol> </li> <li>6. Calculate and interpret the dot product of two vectors.</li> </ol>
	<b>Perform operations on matrices and use matrices in applications.</b>	<ol style="list-style-type: none"> <li>7. Use matrices to represent and manipulate data, e.g., to represent payoffs or incidence relationships in a network.</li> <li>8. Multiply matrices by scalars to produce new matrices, e.g., as when all of the payoffs in a game are doubled.</li> <li>9. Add, subtract, and multiply matrices of appropriate dimensions.</li> <li>10. Understand that, unlike multiplication of numbers, matrix multiplication for square matrices is not a commutative operation, but still satisfies the associative and distributive properties.</li> <li>11. Understand that the zero and identity matrices play a role in matrix addition and multiplication similar to the role of 0 and 1 in the real numbers. The determinant of a square matrix is nonzero if and only if the matrix has a multiplicative inverse.</li> <li>12. Multiply a vector (regarded as a matrix with one column) by a matrix of suitable dimensions to produce another vector. Work with matrices as transformations of vectors.</li> <li>13. Work with <math>2 \times 2</math> matrices as transformations of the plane, and interpret the absolute value of the determinant in terms of area.</li> </ol>

	Domain	Cluster	Standard
<b>Algebra</b>	Sequences and Series (A-S)	Understand and use sequences and series.	<ol style="list-style-type: none"> <li>1. Demonstrate an understanding of sequences by representing them recursively and explicitly.</li> <li>2. Use sigma notation to represent a series; expand and collect expressions in both finite and infinite settings.</li> <li>3. Derive and use the formulas for the general term and summation of finite or infinite arithmetic and geometric series, if they exist.               <ol style="list-style-type: none"> <li>a. Determine whether a given arithmetic or geometric series converges or diverges.</li> <li>b. Find the sum of a given geometric series (both infinite and finite).</li> <li>c. Find the sum of a finite arithmetic series.</li> </ol> </li> <li>4. Understand that series represent the approximation of a number when truncated; estimate truncation error in specific examples.</li> <li>5. Know and apply the Binomial Theorem for the expansion of <math>(x + y)^n</math> in powers of <math>x</math> and <math>y</math> for a positive integer <math>n</math>, where <math>x</math> and <math>y</math> are any numbers, with coefficients determined for example by Pascal's Triangle.</li> </ol>
	Solve Equations and Inequalities (A-REI)	Solve systems of equations and nonlinear inequalities.	<ol style="list-style-type: none"> <li>1. Represent a system of linear equations as a single matrix equation in a vector variable.</li> <li>2. Find the inverse of a matrix if it exists and use it to solve systems of linear equations (using technology for matrices of dimension <math>3 \times 3</math> or greater).</li> <li>3. Solve nonlinear inequalities (quadratic, trigonometric, conic, exponential, logarithmic, and rational) by graphing (solutions in interval notation if one-variable), by hand and with appropriate technology.</li> <li>4. Solve systems of nonlinear inequalities by graphing.</li> </ol>
	Conic Sections (A-C)	Understand the properties of conic sections and apply them to model real-world phenomena.*	<ol style="list-style-type: none"> <li>1. Display all of the conic sections as portions of a cone.</li> <li>2. From an equation in standard form, graph the appropriate conic section: ellipses, hyperbolas, circles, and parabolas. Demonstrate an understanding of the relationship between their standard algebraic form and the graphical characteristics.</li> <li>3. Transform equations of conic sections to convert between general and standard form.</li> </ol>

		Domain	Cluster	Standard
Functions	Building Functions (F-BF)		Build new functions from existing functions.	<ol style="list-style-type: none"> <li>Understand how the algebraic properties of an equation transform the geometric properties of its graph. <i>For example, given a function, describe the transformation of the graph resulting from the manipulation of the algebraic properties of the equation (i.e., translations, stretches, and changes in periodicity and amplitude).</i></li> <li>Develop an understanding of functions as elements that can be operated upon to get new functions: addition, subtraction, multiplication, division, and composition of functions.</li> <li>Compose functions. <i>For example, if <math>T(y)</math> is the temperature in the atmosphere as a function of height, and <math>h(t)</math> is the height of a weather balloon as a function of time, then <math>T(h(t))</math> is the temperature at the location of the weather balloon as a function of time.</i></li> <li>Construct the difference quotient for a given function and simplify the resulting expression.</li> <li>Find inverse functions (including exponential, trigonometric, and logarithmic).               <ol style="list-style-type: none"> <li>Calculate the inverse of a function, <math>f(x)</math>, with respect to each of the functional operations; in other words, the additive inverse, <math>-f(x)</math>, the multiplicative inverse, <math>\frac{1}{f(x)}</math>, and the inverse with respect to composition, <math>f^{-1}(x)</math>. Understand the algebraic and graphical implications of each type.</li> <li>Verify by composition that one function is the inverse of another.</li> <li>Read values of an inverse function from a graph or a table, given that the function has an inverse.</li> <li>Produce an invertible function from a non-invertible function by restricting the domain. Recognize a function is invertible if and only if it is one-to-one.</li> </ol> </li> <li>Explain why the graph of a function and its inverse are reflections of one another over the line <math>y=x</math>.</li> </ol>
	Interpreting Functions (F-IF)		Analyze Functions using different representations.	<ol style="list-style-type: none"> <li>Determine whether a function is even, odd, or neither.</li> <li>Identify or analyze the distinguishing properties of exponential, polynomial, logarithmic, trigonometric, and rational functions from tables, graphs, and equations.</li> <li>Identify the real zeros of a function and explain the relationship between the real zeros and the x-intercepts of the graph of a function (polynomial, rational, exponential, logarithmic, and trigonometric).</li> <li>Identify characteristics of graphs based on a set of conditions or on a general equation such as <math>y= ax^2+ c</math>.</li> <li>Visually locate critical points on the graphs of functions and determine if each critical point is a minimum, a maximum, or point of inflection. Describe intervals of concavity and increasing and decreasing.</li> <li>Graph rational functions, identifying zeros, asymptotes (including slant), and holes when suitable factorizations are available, and showing end-behavior.</li> <li>Solve real world problems that can be modeled using quadratic, exponential, or logarithmic functions* (by hand and with appropriate technology).</li> </ol>
	Trigonometric Functions (F-TF)		Extend the domain of trigonometric functions using the unit circle.	<ol style="list-style-type: none"> <li>Convert from radians to degrees and from degrees to radians.</li> <li>Use special triangles to determine geometrically the values of sine, cosine, tangent for <math>\pi/3</math>, <math>\pi/4</math> and <math>\pi/6</math>, and use the unit circle to express the values of sine, cosine, and tangent for <math>\pi-x</math>, <math>\pi+x</math>, and <math>2\pi-x</math> in terms of their values for <math>x</math>, where <math>x</math> is any real number.</li> <li>Use the unit circle to explain symmetry (odd and even) and periodicity of trigonometric functions.</li> </ol>
	Graphing Trigonometric Functions (G-GT)		Model periodic phenomena with trigonometric functions.*	<ol style="list-style-type: none"> <li>Interpret transformations of trigonometric functions.</li> <li>Match a trigonometric equation with its graph.</li> <li>Determine the difference made by choice of units for angle measurement when graphing a trigonometric function.</li> <li>Graph the sine, cosine, and tangent functions and identify characteristics such as period, amplitude, phase shift, and asymptotes.</li> </ol>

